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Electrical Design for an Electrical System of the Future



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Introduction

We live in a world that seems to go, now more than ever, towards an energy crisis. The traditional power grids have been used in conditions that are a lot different from the ones that were originally designed, causing great stress and deterioration to the system. In their current state, they are not adequate to fit the future needs of the society [1]. This is not the only the reason of why it is needed to change the way we conceive the electricity sector. Relying only on large power stations, far from the place where the electricity is consumed, brings to a huge waste of energy due to transmission losses (only in the United States, losses cost \$70 to \$120 billion a year [2]). Besides transmission losses, wide-scale power outages leave million of peoples and services without electricity every year (see Table 1). Improving the traditional grid can help to reduce them but it is not enough.

| Largest power outages | | | | | |
|-----------------------|---------------------|-----------------|------------------|--|--|
| Location | Date | People affected | Duration | | |
| India | 30-31 July 2012 | 620 millions | From 1 to 2 days | | |
| India | 2 January 2001 | 230 millions | 3 hours | | |
| Bangladesh | 1 November 2014 | 150 millions | 10-12 hours | | |
| Pakistan | 26 January 2015 | 140 millions | 10 hours | | |
| Java-Bali | 18 August 2005 | 100 millions | 7 hours | | |
| Brazil | 11 March 1999 | 97 millions | 4 hours | | |
| Brazil and Paraguay | 10-11 November 2009 | 87 millions | 5 hours | | |
| Turkey | 31 March 2015 | 70 millions | 8 hours | | |
| Northeast America | 14-15 August 2003 | 55 millions | From 1 to 2 days | | |
| Italy | 28 September 2003 | 230 millions | 12 hours | | |

Table 1.1: 10 biggest black-outs in history¹(8 are in the last 15 years).

Global warming, and the resulting climate change, are accepted as undisputed facts by now, even if they are, often, underestimated. The increasing greenhouse gases emissions have been implicated as the main cause of global warming, so the energy sector can play a crucial role in confining it. The environment is asking to make big changes in the way we produce most of the energy we consume, shifting to a cleaner power generation portfolio. The recent improvements and results achieved with renewable sources are astonishing but it is still not enough.





Moreover, many conventional technologies and fossil fuels involved in the electricity

¹Source: Wikipedia ²Source: NASA

2 The electric prosumer community

A prosumer is somebody that is, at the same time, both a consumer and a producer of a certain good. In the energy sector, it is often used to indicate consumers (households, businesses, communities, organizations, etc.) that rely on microgeneration systems to produce electricity and/or combine these with energy management systems, energy storage and electric vehicles [3]. The technologies that revolve around the idea of the electricity prosumer have seen, in the last decades, an outstanding process of improvements and growth. The recent large availability of generating units that offer different sizes at ever lower prices, the increasing potential of storage devices and the proliferation of smart meters devices are helping the figure of the prosumer to spread around the globe. Single renewable generators managed by prosumers that act individually are too small to compete on the market and their supply is unpredictable or inappropriate to satisfy efficiently the demand profile. [9] However, better results can be achieved when prosumers that have the same goals and motivations, located in the same area, are connected together as a community. This group of people is what is called an Electric Prosumer Community (EPC). Many drawbacks and challenges are encountered at various levels when thinking about the concept, from the development of solid regulations to the expedients to make it an economically advantageous alternative to traditional strategies. Co-ordinating efficiently the interests of every member of the community can be difficult and disagreements among members are very likely to occur [5]. The following sections present some popular techneologies to produce and store energy, along with some possible goals to be pursued by the community.

2.1 Generation

The revolution brought by renewable energies has already passed its early stage and it has started to be taken seriously by almost everyone. Even though most of the established goals are not yet reached, the transition to a low-carbon economy seems, now, less distant than before. The total installed power capacity associated to renewable sources reached 2 millions of MW at the end of 2016 [6] providing, in the same year, the 24.5 % of the global electricity production [7]. Renewables are breaking records after records. In March and April 2017, renewable generation surpasses nuclear in the U.S. for the first time since 1984 [10]. One month later, in Italy, renewable sources produced more than the 87% of the total demand of one day [11]. And these are just some of the many recent milestones hit by renewable power. Even if they are not the only option, renewables and eco-friendly generators have become one of the first things that comes to mind when people talk about small, distributed generating units, and thus, micro grids and electric prosumer communities. The most promising and widespread technologies for current microgeneration systems are: • Solar PV panels; • Micro-wind turbines; • Micro Combined Heat and Power (micro-CHP); • Fuel cells; • Micro turbines; They and some of their characteristics will be now introduced.

2.1.1 Solar photovoltaic

Solar photovoltaic (PV) panels are usually considered as the face of the "renewable revolution". The electric capacity of solar PV installed has been, in 2016, bigger than any other generation technology [15] (the total capacity has crossed the 300 GW [12]). Residential solar PV systems are now as much as 70% cheaper than in 2008 [14]. In Germany, prices for a typical 10 to 100 kWp PV residential rooftop-system were around 14,000 e/kW p in 1990. At the end of 2016, such systems cost about 1,270 e/kW p. As regards the Energy Payback Time of a solar photovoltaic system, it is strongly dependent from the location: in the Northern Europe it is less than 3 years, while in the South it is around 1.5 years (in Sicily a new PV installation has a PBT of 1 year)

| Parameter Value | | Reference | | | |
|---------------------------------|------------------------------------|---------------|--|--|--|
| European Union / Worldwide | | | | | |
| PV market | 7.3 / 77.3 GW | IHS | | | |
| Cumulative installation | 106 / 320 GW | IEA+IHS | | | |
| PV power consumption | 114.4 / 333 TWh | BP | | | |
| PV electricity share | 3.4 / 1.3 % | BP | | | |
| Worldwide | | | | | |
| Record solar cell efficiency: | | | | | |
| III-V MJ / mono-Si / multi-Si / | 46.0 / 26.7 / 21.9 / 21.7 / 21.0 % | Green and al. | | | |
| CIGS / CdTe | | | | | |
| Germany | | | | | |
| Price PV rooftop system | ≈ 1500 €/kWp | BSW | | | |
| LCOE PV power plant | ≈ 0.08 €/kWh | ISE & Agora | | | |

Table 2.1: Data about photovoltaics installation [16]

There is also a less popular type of solar panels that integrates PV panels with solar collector, called PV/T collector. Besides the merit of producing also thermal energy, the presence of the solar collector lowers the temperature of the above PV panels, increasing their electrical efficiency. The main shortcoming is in their price, since they are more expensive than traditional solar PV systems.

2.1.2 Small wind Turbines

In the last decade, the interest in wind turbines has continued to increase enormously worldwide. Competition in the market and better performances reduced the capital costs, making them a competitive alternative to produce electricity, even when compared with traditional power plants. Promising new designs are characterized by rotors much larger than before, since the capacity factor increases with the size. Large scale wind farms, both onshore and offshore, can provide exceptional results when placed in the right location, but their range of size and power usually do not fit the requirements and the resources of an EPC. Residential and smaller users needs can be tackled with smaller systems that work with the same principles. These small wind turbines or micro-wind turbines, whose power ratings are around few kW, can help to satisfy (at least partially) the domestic demand, especially if installed together with other generating units. Despite their potential, small wind turbines present many shortcomings: the efficiency of these devices is smaller then the one of common wind turbines, the problem of noise production becomes very relevant inside a neighborhood and suburban locations offer, in most of the cases, only low wind speed with high turbulence. These characteristics make small wind turbines difficult to get accepted by the public opinion .

2.1.3 Micro-CHP

Cogeneration is the production, at the same time, of two forms of energy, usually electricity and heat. It is an old concept and it can be found applied even in early power plants. The recent growing interest by consumers (and investors) in sustainability and, gave an additional boost to cogeneration because, even when it does not involve renewable energy sources, it represents a very efficient way to reduce carbon emissions. Moreover, it allows to save an incredible amount of money. Combined heat and power system can be also designed at smaller scales (Micro-CHP), making it an attractive option to implement in EPCs. Another advantage of cogeneration is that it can be applied with a large range of (renewables and non-renewables) generation systems.

Micro turbines

Among the distributed generation technologies that do not rely on renewable sources, there is one that fits very well the characteristics of the EPCs: micro turbines. Microtusbines are basically small versions of the combustion turbines that can be found in power plants. Their output can go from 10 kW to a few hundred of kW [18]. The main advantages are the tolerable costs, the good efficiency,

the easy installation and a high reliability. A wide range of models with different features are available on the market. Most of them are powered by fuels like natural gas or diesel and, unlike PV panels or wind turbine, can be started whenever it is needed. The use of fuel in micro turbines becomes more efficient when the device is integrated in a co-generation (CHP) system, achieving efficiency up to 80%. In this case, the thermal energy produced by the turbine is no more wasted, but it can be used for heating.

Fuel cells

Another option to generate power inside an EPC is represented by fuel cells. Fuel cells are devices that convert the chemical energy of a fuel into electrical energy [29] and can be easily integrated into CHP systems. They are usually compared to batteries since the conversion is performed by electrochemical processes, but they differ in the fact that fuel cells require a fuel to flow through them. There are a lot of different fuel cells and most of them represents an eco-friendly option to generate energy with a good efficiency. Their market is growing rapidly, researchers are developing more and more technologies. Among the current available fuel cells, phosphoric acid fuel cells (PAFC), molten carbonate fuel cells (MCFC), and solid oxide fuel cells (SOFC) are the ones most recommended for an EPC [1].

2.1.4 Other technologies

What has been presented in this section is only a small part of the available technologies for distributed generation (DG). Many other techniques used to produce electric energy in large power plants can be applied also at smaller scales. Sustainable alternatives such as small hydroelectric plants, geothermal energy or biomass resources can be feasible option in some cases. Every one of them is characterized by advantages and disadvantages and it is not possible to affirm which one the best since it depends on countless parameters. A good suggestion on how to produce energy in the community is to rely on more than just one technology: hybrid systems are a good method to compensate for the shortcomings of one technology with the advantages of another one, increasing the production reliability.

2.2 Storage

Renewable distributed generators are not perfect. Many flaws that are often ascribed to these technologies are, for example, the lack of high reliability, the limited power quality and the difficulties to predict and organize the production. An expedient that helps to mitigate these problems is the integration in the network of efficient energy storage systems (ESS). Besides the benefits that they offer to renewable generators, they are however a powerful tool to manage energy in a clever way. EES can be classified according to the form of energy they involve: we can have electrochemical, thermal, chemical, electrical or mechanical devices. Electrochemical batteries are

what is popularly associated to the concept of energy storage, due to their presence in many common applications. Batteries store energy under the electrochemical form and saw their origin at the beginning of the 19th century. Since then, countless technologies appeared, increasing the capacity, the power density, the lifetime, etc. The last decades saw new remarkable improvements, making batteries less expensive and more suitable for residential usage [19] [29]. Even though batteries are very popular, the 96% of the electrical storage capacity installed in the world is represented by another kind of system: the pumped hydroelectric energy storage (PHES) [29]. PHES uses the gravitational energy of a reservoir of water located at a certain elevation. When an electrical demand is required, the water is sent to a lower reservoir, flowing through turbines that produce electricity. Depending on the case, some communities could implement smaller PHES system for seasonal storage. Many other technologies are available for EES, such as compressed air energy storages (CAES), flywheels and supercapacitors, but they still present major shortcoming and are suited only for particular applications. A summary of the characteristics of some of the energy storage technologies is presented in Fig. 2.2.

| Туре | Energy Density | Power Density | Response Time | Cycling Times |
|----------------|----------------|---------------|---------------|---------------|
| | Wh/kg | W/kg | | |
| Flywheel | 5-30 | 400-1500 | 1 s | Above 20,000 |
| Compressed air | 30-60 | - | 1-10 min | Above 100,000 |
| Lead-acid | 30-50 | 75-300 | 10 s | 2000 |
| Lithium-ion | 75-200 | 150-300 | 10 s | 10,000 |
| Sodium-sulfur | 100-250 | 100-230 | 10 s | 2500-6000 |
| Supercapacitor | 5-10 | 5-10 | 1 s | 100,000 |

Table 2.2: Energy storage technologies [19]

2.2.1 Electric Vehicles

There is another element, besides renewables, that promises to help the shift to a cleaner environment and the building of a more sustainable future: Electric Vehicles (EVs). Besides the effects that they can have on the automotive industry, EVs can be a powerful tool into the pocket of the electric grid, providing or storing power upon request when plugged in: this concept is called Vehicle-to-Grid power (V2G) [20]. Utility fleets seem to have a good economic potential as ancillary service for the power grid [21], but also individual vehicles could be exploited if used as storage devices in an EPC. Their implementation in a micro grid is more difficult than the common battery's one, but they still can provide interesting features and additional capacity

[22]. 2.3 Demand

The cleanest energy is the one that you do not use, we all know it. Reducing the energy consumption would be probably the most efficient way to contrast pollution and global warming, but it is not always feasible in practice. One of the key points of an EPC is trying to satisfy the internal demand of the prosumers in an efficient way. Not an easy task, since forecasting future demand and production is extremely difficult, and in some cases, impossible. When more

consumers join together in the same community, however, it would be possible to coordinate and to organize some of the energy consuming tasks in order to reduce total consumption, peak demand and costs. This approach is called "demand management" (from the demand-side).

2.4 A goal-oriented community

The concept itself of a community of multiple electric prosumers implies that they intend to pursue a set of mutual goals. Since EPCs are still in their early state and since there is a lack of regulations, it is not perfectly clear what the policy of a community could be. The objective of the community can be, for example, to maximize the consumption of "green" power produced by the distributed generators, to minimize the exchanges with the feeder or to optimize the overall costs of the entire community [24]. Whatever the goal is, however, there are very few studies that analyze the energy sharing between prosumers and there seems to exists no techniques yet to identify prosumers that do not act as agreed [25]. Investigating further on these aspects is crucial for the development of new EPCs.

3 A control scheme for the community

Since their conception, micro grids have been deeply examined in literature (see for example [26] - [28]) and many challenges and shortcomings have been detected. Monitoring and controlling the network can be extremely difficult, representing an interesting argument for research. The dynamics of electric power system are complex even at smaller scales, due to the many parameters that have effect on the system. The safety of the network is not the only thing that matters, the economic side of the problem is very relevant too. Therefore, this work will focus on how to control the prosumers' operation inside the community, trying to ensure the safety of the grid while pursuing a common objective.

3.1 Formalising the prosumer community

Before looking further in the control challenges, it is better to try to formalize a simplified model of the prosumer community dynamics to use in the design of a decentralized control scheme. We consider a low-voltage distribution network composed by $N \in N$ buses, where one bus is the root connection, the point of connection between the community and the power system, while the remaining N - 1 buses are the Npro \in N prosumers' dwellings inside the EPC. The number of branches in the network is $L \in N$, with Rl and Xl as, respectively, the resistance and the reactance of the l - th branch ($l \in \{1 ... L\}$). For simplicity we will

consider a linear network like the one in Fig.3.1, with batteries and solar photovoltaic panels installed at each prosumer bus.



Figure 3.1: Simplified representation of the electric prosumer community

As previously stated, each prosumer inside the community can consume, produce or store electricity. We can associate therefore a generation capacity Xpr, i , a storage capacity Xbatt, i , a storage charging efficiency η ch, i and a storage discharging efficiency η dis, i to each bus $i \in \{1, \ldots, N - 1\}$. We consider the community behavior over a set of discrete time steps $t \in \{1, \ldots, T\}$ with $T \in N$ as the time horizon. Please note that all the quantities are assumed to be in per unit and all the power related variables assume the average value over the time interval Δt between two time steps. At each time step $t \in \{1, \ldots, T\}$ the prosumer $i \in \{1, \ldots, N - 1\}$ consumes the active power P t load, i and the reactive power P t load, i . The load consumption depends on the electrical appliances located and used inside the dwelling and, in the context of this work, we consider that it can not be modulated by the control system. What can be directly controlled by the prosumer is the power production (active P t pr, i and reactive Q t pr, i) and the power exchanged with the batteries (stored P t ch, i or drawn P t dis, i). The power produced is capped by the maximal potential that the technology involved and the weather condition allow:

$$P_{pr,i}^t \le P_{pr,i}^{t,max}$$

$$\left|Q_{pr,i}^{t}\right| \leq Q_{pr,i}^{t,max}$$

The battery at bus i is characterized at every time step by the energy stored S t i . The two variables related to the power exchanged with the batteries, P t ch, i (power charging the battery) and P t dis, i (power discharging the battery), are both always positive. The net power exchanged with the device cannot exceed a limit that mainly depends on the storage device and cannot cause the state of charge of the battery to go to values smaller

than 0 or higher than 1. The battery dynamics is described in the following equations: P t ch, i - P t dis, $i \le P$ t, max batt, i (3.3) $0 \le S$ t batt, $i + \eta$ ch, i P t ch, $i\Delta t - P$ t dis, i η dis, i $\Delta t \le X$ batt, i (3.4) We denote with P t δ , i and Q t δ , i the power injected in the distribution network from prosumer i at time t. P t δ , i = P t pr, i + P t dis, i - P t ch, i - P t load, i (3.5) Q t δ , i = Q t pr, i - Q t load, i (3.6) When these variables are different from zero it means that the prosumer i has a surplus (if P t δ , i > 0) or a deficit of power (if P t δ , i < 0). In these cases, it need to be balanced by the surplus/deficit of another prosumer inside the community or by the feeder. The control of the power production and the usage of the batteries is a crucial element to reduce overvoltages, line overloading, network losses and costs. Speaking about costs and revenues, we assume that the power exchanges between prosummers are not associated to any expense (their price is zero) while the energy exchanged by a prosumer with the retailer at time t is characterized by a price c t el.

3.2 Decentralized control scheme

Like other system composed by multiple agents, there are two main control strategies for an EPC, a centralized and hierarchical mechanism or a distributed scheme. A centralized control scheme indicates that all the data possessed are gathered together and sent to a central entity that computes the orders and coordinates the prosumers' actions. In order to achieve good results, this entity should have a detailed model of the network, efficient communication devices and the equipment required to receive, store and process the information. The latter is called "Micro grid Central Controller" (MGCC) and plays a fundamental role in the control structure. The main shortcoming of building and maintaining all the machinery involved in the centralized strategy is that it can be very expensive. Morover, since current smart meters technologies appeared on the market, privacy concerns for the single prosumer are rised due to the sharing of personal consumption information with other people [8]. We still do not know how a future regulation will treat this matter

once the figure of prosumers will spread, therefore it could be interesting to investigate possible designs for decentralized control schemes that do not require the individual to share too much information. With "decentralized control scheme" we imply that each single prosumer in an EPC takes autonomous decisions on how to interact with the rest of the network. We want to investige how to design distributed control schemes that may contribute to reach (at least partially) the objectives of the community. In order to avoid that prosumers share privacyrelated information, we suppose that they compute their decisions only relying on local measurements. This is not an easy task, since a partial knowledge of the state of the network makes difficult for to compute cost-effective decisions. Not only, the revenues are difficult to maximize, but unappropriated actions can cause overvoltage, under voltages or over loadings inside the network, undermining the safety of the micro grid. Our strategy is to resort to supervised learning techniques that may extract, from centralized, optimal solutions, decision making patterns to be applied at the level of the single prosumer.

3.3 Supervised learning algorithm

Supervised learning (SL) methods have their roots in statistics world. Their main goal is to predict what the output Ψ of a set of inputs ψ is, analyzing the characteristics of the training data [36]. SL techniques are used in many areas and problems. If the outputs are some sorts of labels, we call it a classification problem, otherwise, if the outputs consist of continuous variables, it is a regression problem. Each problem involving Supervised Learning includes, indeed, a training process, that is performed using a data-set of samples that contains a set of inputs and their corresponding outputs. The SL algorithm examines these data, tries to learn from them and produce an estimation function to find the output associated to new inputs. Literature is full of SL methods and algorithm to apply to several problems. One popular family of SL techniques is the one of the tree-based methods, simple to apply and suitable for both classification and regression problems [36]. Some common tree-based methods are CART (Classification and Regression Trees) [30], Tree Bagging and Random Forest [38]. The accuracy of these models depend on the particular problems on which they are applied, but in several cases the results are slightly the same. The model used in the development of the decentralized control strategy is another tree-based method called Extremely Randomized Trees.

3.3.1 Estimators

In order to try to predict the optimal strategy of a prosumer, we train four different estimators. These four estimators are RP,RQ,RC and RD and they are dedicated, respectively, to the optimal levels of active power production, reactive power production, power charging the storage device and power discharging the storage device. Each estimator is constructed to take as input the set of data only related to the local prosumer i at timestamp t.

Training

The training of estimators in the supervised learning problem is performed passing to the model a set of data containing several samples of optimal (input, output) pairs. The estimator, observing this data, extracts from them a strategy to predict which should be the right output to associate to a certain input. To find the decision making patterns to be applied locally by the prosumers, the four estimators RP,RQ,RC and RD are trained using the solution of optimal power flow problems, solved by a centralized "omniscient" scheme, set in the same network that the estimators should deal with. Several methods exist to solve such problems, one of them, suited for our case is described in chapter 4. This centralized controller has a perfect knowledge of the problem and it can thus detect the decisions that optimize the global objective of the EPC. Solving one such problem outputs a time series of data, corresponding to the evolution of all the indicators over the time horizon:

$$[\Xi_0^*, \dots, \Xi_{T-1}^*]$$
 (3.7)

From this time series of data, one can extract a series of local data, i.e. relative to one single prosumer (i):

$$\left[\Xi_{1}^{(i),*},\ldots,\Xi_{T}^{(i),*}\right]$$
 (3.8)

where $\forall t \in \{1, ..., T\}, \forall i \in \{1, ..., N-1\},\$

$$\Xi_{i}^{t,*} = \begin{pmatrix} P_{pr,i}^{t} & Q_{pr,i}^{t} \\ P_{pr,i}^{max,t} & Q_{pr,i}^{max,t} \\ P_{pr,i}^{t} & Q_{pr,i}^{t} \\ P_{Load,i}^{t} & Q_{Load,i}^{t} \\ P_{ch,i}^{t} & P_{dis,i}^{t} \\ S_{batt,i}^{t} & c_{el}^{t} \\ \left| \underline{\mathbf{y}}_{i}^{t} \right| & arg(\underline{\mathbf{y}}_{i}^{t}) \end{pmatrix},$$
(3.9)

From these extractions, we generate the following learning sets:

• To generate a learning set dedicated to learning how to optimize the level of active power production, we process the whole variables Ξ t,* i into the following set of (input, output) pairs:

$$\mathcal{L}^{P} = \left\{ \left(\psi_{P,i}^{t}, \Psi_{P,i}^{t} \right) \right\}_{i=1,t=1}^{i=N-1,t=T}$$
(3.10)

where, $\forall t \in \{0, ..., T - 1\}, \forall i \in \{1, ..., N\},\$

$$\psi_{P,i}^{t} = \left(i, t, c_{el}^{t}, \left|\underline{\mathbf{v}}_{i}^{t}\right|, arg(\underline{\mathbf{v}}_{i}^{t}), P_{Load,i}^{t}, Q_{Load,i}^{t}, P_{pr,i}^{max,t}, Q_{pr,i}^{max,t}, S_{batt,i}^{t}\right)$$
(3.11)

$$\Psi_{P,i}^t = P_{pr,i}^t \tag{3.12}$$

Where:

- *i* : id number of the bus considered;
- t : time-step considered;
- $-|\underline{\mathbf{v}}_{i}^{t}|$: magnitude of the voltage at bus *i* at time step *t*;
- $arg(\underline{v}^{t})$: phase of the voltage at bus *i* at time step *t*;
- c_{el}^{t} : electricity price at time step t;
- $S_{batt,i}^{t}$: level of charge of the storage of bus *i* at time step *t*;
- $P_{Load,i}^{t}$, $Q_{Load,i}^{t}$: active and reactive power consumption at bus *i* at time step *t*;
- $P_{pr,i}^{max,t}$, $Q_{pr,i}^{max,t}$: maximal active and reactive production potential at bus *i* at time step *t*;
- To generate a learning set dedicated to learning how to optimize the level of reactive power production, we process the whole variables \(\mathbb{\Sigma}_i^{t,*}\) into the following set of (input, output) pairs:

$$\mathcal{L}^{Q} = \left\{ \left(\psi_{Q,i}^{t}, \Psi_{Q,i}^{t} \right) \right\}_{i=1,t=1}^{i=N-1,t=T}$$
(3.13)

where, $\forall t \in \{0, ..., T - 1\}, \forall i \in \{1, ..., N - 1\}$:

$$\psi_{Q,i}^{t} = = \psi_{P,i}^{t}$$

$$\Psi_{Q,i}^{t} = = Q_{pr,i}^{t}$$

 For generating a learning set dedicated to learning how to optimize the level of power injected into the battery, we process the whole variables \(\mathbb{\Sigma}_t^{(i),*}\) into the following set of (input, output) pairs:

$$\mathcal{L}^{C} = \left\{ \left(\psi_{C,i}^{t}, \Psi_{C,i}^{t} \right) \right\}_{i=1,t=1}^{i=N-1,t=T}$$
(3.14)

where, $\forall t \in \{0, ..., T - 1\}, \forall i \in \{1, ..., N - 1\}$:

$$\psi_{C,i}^{t} = = \psi_{P,i}^{t}$$

$$\Psi_{C,i}^{t} = = P_{ch,i}^{t,*}$$

 To generate a learning set dedicated to learning how to optimize the level of power injected into the battery, we process the whole variables \(\mathbb{\Sigma}_i^{t,*}\) into the following set of (input, output) pairs:

$$\mathcal{L}^{D} = \left\{ \left(\psi_{D,i}^{t}, \Psi_{D,i}^{t} \right) \right\}_{i=1,t=1}^{i=N-1,t=T}$$
(3.15)

where, $\forall t \in \{0, ..., T-1\}, \forall i \in \{1, ..., N-1\}$:

$$\psi_{D,i}^{t} = = \psi_{P,i}^{t}$$

$$\Psi_{D,i}^{t} = = P_{dis,i}^{t}$$

The learning sets should be obtained from scenarios similar to those that the actual network could deal with and it should contain a large number of (input, output) pairs. The set of network data included in the input ψ t P,i , ψ t Q,i , ψ t C,i , ψ t Q,i of the estimators RP,RQ,RC and RD could be different from the one presented. Data like the voltage or the power production at the neighbors' buses have been neglected in order to avoid privacy concerns. Information like the period of the year (contained in the value of t) or the phase of the voltage could seem, instead, useless, but preliminary tests showed that they can help the quality of the predictions.

3.3.2 Post-processing the prediction

Once the estimators are trained they can be used to try to predict the decision of the single prosumer when it dynamically interacts with other prosumers and the retailer. The idea is to pass to the estimators RP,RQ,RC and RD local measurements referred to a prosumer i (the same kind of inputs used to train them) and to use their predictions to control the choices of that prosumer. Since there are no constraints to the values of the outputs, their prediction could lead to impracticable or dangerous actions, (i.e. the estimator suggest a power production greater then the potential one or a power injected in the storage that would bring the charge of the battery beyond the maximum value that it allows). Therefore a partial post-processing of the outputs is needed to change the value. We denote with R P* i,t , R Q* i,t , R C* i,t and R D* i,t the preliminary predictions made by the estimators associated to the input of bus i and time step t. The actual actions at the same bus and time step are corrected to P t pr, i , Q t pr, i , P t ch, i and P t dis, i as follows: • For the active power production level:

 $\begin{aligned} \text{if } & \mathcal{R}_{i,t}^{P*} \geq P_{pr,i}^{max,t} \\ & P_{pr,i}^{t} = P_{pr,i}^{max,t} \\ \text{else if } & \mathcal{L}^{P}\left(in^{i,t}\right) \leq P_{pr,i}^{min,t} \\ & P_{pr,i}^{t} = P_{pr,i}^{min,t} \\ \text{else } & P_{pr,i}^{t} = \mathcal{R}_{i,t}^{P*} \end{aligned}$

· For the reactive power production level:

if
$$\mathcal{R}_{i,t}^{Q*} \ge Q_{pr,i}^{max,t}$$

 $Q_{pr,i}^{t} = Q_{pr,i}^{max,t}$
else if $\mathcal{L}^{Q}(in^{i,t}) \le Q_{pr,i}^{min,t}$
 $Q_{pr,i}^{t} = Q_{pr,i}^{min,t}$
else $Q_{pr,i}^{t} = \mathcal{R}_{i,t}^{Q*}$

• For the power injected in the battery:

$$\begin{aligned} \text{if } \mathcal{R}_{i,t}^{C*} &\geq P_{batt,i}^{max} \\ P_{c,i}^{t} &= P_{pr,i}^{max,t} \\ \text{else if } \mathcal{R}_{i,t}^{C*} &\leq 0 \\ P_{ch,i}^{t} &= 0 \\ \end{aligned} \\ \begin{aligned} \text{else } P_{ch,i}^{t} &= \mathcal{R}_{i,t}^{C*} \\ \text{if } S_{i}^{t} + P_{ch,i}^{t} \eta_{ch,i} &\geq X_{batt,i} \\ P_{ch,i}^{t} &= \frac{X_{batt,i} - S_{i}^{t}}{\eta_{ch,i}} \end{aligned}$$

· For the power drawn from the battery:

$$if \ \mathcal{R}_{i,t}^{D*} \ge P_{batt,i}^{max}$$

$$P_{dis,i}^{t} = P_{pr,i}^{max,t}$$

$$else \ if \ \mathcal{R}_{i,t}^{D*} \le 0$$

$$P_{dis,i}^{t} = 0$$

$$else \ P_{dis,i}^{t} = \mathcal{R}_{i,t}^{D*}$$

$$if \ S_{i}^{t} - \frac{P_{dis,i}^{t}}{\eta_{dis,i}} < 0$$

$$P_{dis,i}^{t} = S_{i}^{t}\eta_{dis,i}$$

It is important to notice that, even after post-processing the output values, there is still risk of incurring in under-voltages/over-voltages.

4 The Power flow analysis

The study and operation of any interconnected electric power system require to perform a numerical analysis to determine the electrical state of the network starting from parameters that are known: this computation is called power flow analysis or load-flow study. Power flow analysis allows to compute currents, real and reactive power flowing in the branches, losses, voltages at the buses. It is used not only to analyze the operation of networks that already exist, but is a powerful method also to find what configurations lead to critical conditions or to design new power systems. Moreover it can be included in other methods to perform unit commitment, economic dispatch or to determine the optimal power flow, the most efficient configuration of the system. This chapter presents a basic formulation of the problem and a method to solve it when applied to an EPC.

4.1 AC Power flow equations

Defining and solving the power flow equations of the power system are the main tasks in the load flow study. One of the data required to perform it is the nodal admittance matrix YBUS. In a system of N buses, YBUS is a $N \times N$ matrix such that:

VYBUS = I

Eq. (4.1) is the matrix form of the well-known Ohm's Law. There are four different variables associated to each bus $i \in \{0, ..., N-1\}$: the active power injection Pi, the reactive power injection Qi, the voltage magnitude Vi and the voltage phase θi . Depending on the type of the bus i, the variables that are assumed to be known are:

- if the bus i is the slack bus, the voltage magnitude Vi and phase θi ;
- if the bus i is a P-V bus, the voltage magnitude Vi and the active power injection Pi ;
- if the bus i is a P-Q bus, the active power Pi and reactive power Qi injections;

The purpose of the analysis is to evaluate the remaining:

- NP-V + NP-Q voltage phases;
- NP–Q voltage magnitudes;

The total unknowns are thus NP–V + 2NP–Q. For each bus $i \in \{0, ..., N - 1\}$ we can write the following power balance equations:

$$P_{i} = \sum_{j=0}^{N-1} V_{i} V_{j} \left(G_{ij} cos \left(\theta_{i} - \theta_{j} \right) + B_{ij} sin \left(\theta_{i} - \theta_{j} \right) \right)$$
(4.2)

$$Q_{i} = \sum_{j=0}^{N-1} V_{i} V_{j} \left(G_{ij} sin \left(\theta_{i} - \theta_{j} \right) - B_{ij} cos \left(\theta_{i} - \theta_{j} \right) \right)$$
(4.3)

Where:

- Gi j is the real part of the element corresponding to the ith row and jth column in the YBUS ;
- • Bi j is the imaginary part of the element corresponding to the ith row and jth column in the YBUS.

We have therefore a set equations that we can use to find the unknown variables. Once the values of these variables are found, the evaluation of the remaining parameter of interest (i.e.: current in the branches, power losses, etc.) becomes trivial, using other theoretical relationships such as:

$$\mathbf{I}_i = \left(\frac{P_i + jQ_i}{V_i}\right)^{\prime}$$

4.2 Optimal Power Flow in an EPC

The power flow study can be implemented in an optimization problem to look for the most efficient way to operate a power system while respecting the network operating limits and other constraints. This problem is commonly referred as the Optimal Power Flow (OPF).

The set of equations described in Section 4.1 involves non-linear relationships. The resulting optimization al problem is non-linear and non-convex, increasing exponentially the computational cost required to solve the OPF, especially with large interconnected power systems. There are many methods to solve it and multiple approaches have been developed to decrease the complexity of the problem (i.e. "Direct Current Power Flow" [31] and "Fast Decoupled Load Flow" [32]). The assumptions that most of these models require, however, do not always fit with low-voltage (LV) distribution networks. An interesting method with good convergence properties that well matches with LV networks is the one developed by Fortenbacher and al. [33]. In this paper, the authors recast the non-linear power flow equations into a linear problem, relying on assumptions that are common to most LV networks. This linear problem is iteratively solved, updating each time the voltages at the buses with a combined forward backward sweep technique (FBS) [34]. This method is called Forward-Backward Sweep Optimal Power Flow (FBSOPF) and it will be used, in the context of this work, to represent a centralized "ominiscient" control strategy and to create the learning sets used by SL model presented in Section 3.3. Its formulation will now be resumed and explained.

4.2.1 The FBS-OPF algorithm

Let's consider a low-voltage distribution network with a weakly meshed radial structure similar to the one formalized in the previous chapter, composed by $N \in N$ buses, where the first bus is the Point of Common Coupling (PCC) between the main grid and the microgrid, while the remaining N - 1 buses are the Npro $\in N$ prosumers' houses of the electricity prosumer community. Every relationship that follows is written for a generic time step t and are valid $\forall t \in \{1, ..., T\}$ with T as the time horizon of the problem. The topology of the network is mapped by the bus-injection to branch current matrix $Mf \in R L \times N$ defined in [34]. It links the vector i $t \in R N \times 1$ of the bus current injections to the vector i $t b \in R L \times 1$ of the branch currents through the Kirchhoff's Current Laws.

$$\underline{i}_{b}^{t} = M_{f} \underline{i}^{t}$$

For example, if we consider the following simple network:



We can write:

$$i_{b1} = i_1 + i_2 + i_3$$

 $i_{b2} = i_2$
 $i_{b3} = i_3$

From eq. 4.5 we have that M_f is equal to:

$$\mathbf{M}_{f} = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

The formulation of the FBS-OPF requires also the introduction of another matrix, indicated with M ∈ R L × N-1 that is obtained deleting the first row from Mf . To convert the traditional OPF into a linear problem we need now to make some approximations about voltages, currents and losses. Approximating the voltages If we consider a generic branch l ∈ { 1 . . . L } we can write, according to

Ohm's Law, that the voltage drop in the line is:

$$\Delta \underline{v}_{l}^{t} = [R_{d1} + j X_{dl}] \underline{i}_{bl}^{t}$$

Merging eq. 4.6, 4.4 and 4.6 we can write in a matricial form:

$$\Delta \underline{\boldsymbol{\nu}}^{t} = \boldsymbol{M}^{T} \left[\boldsymbol{R}_{d} + j \boldsymbol{X}_{d} \right] \boldsymbol{M}_{f} \underline{\boldsymbol{V}}_{df}^{t} \left[\boldsymbol{P}_{gen}^{t} + j \boldsymbol{\mathcal{Q}}_{gen}^{t} \right]^{*}$$

- Rd = diag { Rd 1 . . . Rd L} \in R L×L is the resistance matrix;
- Xd = diag { Xd 1 . . . Xd L} ∈ R L×L is the reactance matrix;
- V t d f = diag $1 v t 0 \dots 1 v t N \in R N \times N$ is nodal line to neutral voltages matrix.

Eq.(4.7) presents a complex relationship. To linearize it, the authors of the paper [33], decide to assume that nodal voltage angles are small and resistances in the network are way bigger than its reactance's. This assumptions is usually true for LV networks. We can approximate then Eq.(4.7) as:

$$\mathbf{v}^{t} \approx \mathbf{v}_{s} + \begin{bmatrix} \mathbf{M}^{T} \mathbf{R}_{d} \mathbf{M}_{f} \left| \underline{\mathbf{V}}_{df}^{t} \right| & \mathbf{M}^{T} \mathbf{X}_{d} \mathbf{M}_{f} \left| \underline{\mathbf{V}}_{df}^{t} \right| \end{bmatrix} \begin{bmatrix} \mathbf{P}_{gen}^{t} \\ \mathbf{Q}_{gen}^{t} \end{bmatrix}$$

The matrix $\begin{bmatrix} M^T R_d M_f \left| \underline{V}_{df}^t \right| \quad M^T X_d M_f \left| \underline{V}_{df}^t \right| \end{bmatrix}$ is called \mathbf{B}_v^t and $v_s \in \mathbb{R}^{L \times 1}$ is the slack bus voltage vector.

Approximating

the currents in the branches Another assumption that we can make for LV networks is that reactive power injections are usually small if compared with active power injections. Assuming that, we express current in the branches as:

$$i_b^t \approx M_f \left| \underline{V}_{df}^t \right| P^t$$

The product $M_f \left| \underline{V}_{df}^t \right|$ is denoted as \mathbf{B}_r^t .

Approximating the losses

The power losses are approximated as linear piecewise function:

$$\mathbf{P}_{Loss} \approx max\{\mathbf{L}_0^t\mathbf{P}^t, -\mathbf{L}_0^t\mathbf{P}^t, \mathbf{L}_1^t\mathbf{P}^t + \mathbf{b}^t, -\mathbf{L}_1^t\mathbf{P}^t + \mathbf{b}^t\}$$
$$\mathbf{Q}_{Loss} \approx max\{\mathbf{L}_0^t\mathbf{Q}^t, -\mathbf{L}_0^t\mathbf{Q}^t, \mathbf{L}_1^t\mathbf{Q}^t + \mathbf{b}^t, -\mathbf{L}_1^t\mathbf{Q}^t + \mathbf{b}^t\}$$

Where:

- $\mathbf{L}_{0}^{t} = diag\{i_{0}^{0,t}, \ldots, \mathbf{1}_{l}^{0,t}\}\mathbf{R}_{d}\mathbf{M}_{f}\left|\underline{\mathbf{V}}_{df}^{t}\right|$
- $\mathbf{L}_1^t = diag\{i_0^{0,t} + i_0^{1,t}, \dots, i_l^{0,t} + \mathbf{1}_l^{1,t}\}\mathbf{R}_d\mathbf{M}_f \left| \underline{\mathbf{V}}_{df}^t \right|$
- $\mathbf{b}^{t} = -\left[r_{d1}i_{0}^{0,t}i_{0}^{1,t}, \dots, r_{dl}i_{l}^{0,t}\mathbf{1}_{l}^{1,t}\right]$
- $i^{0,t} = 0.25 \mathbf{M}_f \mathbf{P}^{max,t}$
- $i^{1,t} = 0.75 \mathbf{M}_f \mathbf{P}^{max,t}$

A graphic representation of the loss approximation for a two bus system is showed in Fig. (4.2.1).



Figure 4.1: Example of the loss approximation in a line between two buses [33].

Battery dynamics

If there are storage devices in the network, we need to introduce additional equations to model their dynamics. A possible way to describe the time-varying level of charge of the battery at bus $i \in \{1, ..., N-1\}$, $\forall t \in \{2, ..., T\}$ is:

$$S_{batt,i}^{t} = S_{batt,i}^{t-1} + \eta_{ch,i} P_{ch,i}^{t-1} - \frac{P_{dis,i}^{t-1}}{\eta_{dis,i}}$$

Where $\eta_{ch,i}$ and $\eta_{dis,i}$ are the efficiency of the battery for the charge and discharge processes. The initial charge of the battery, $S_{batt,i}^{1}$, is usually fixed to 0.

Power balance The most important constraint of the OPF problem is to satisfy the power balance inside the network, expressed as:

$$\sum_{i=0}^{N-1} P_{gen,i}^{t} - \sum_{j=1}^{L} P_{los,j}^{t} - \sum_{j=1}^{L} Q_{los,j}^{t} - \sum_{i=0}^{N-1} P_{load,i}^{t} = 0$$

Network physical limits

Any solution proposed by the optimization problem must respect the physical limits related to power production and consumption, avoiding over voltages, under voltages, overloadings and that the state of charge of the batteries remains between a minimum and a maximum value. These constraints can be written as:

$$\begin{aligned} -\mathbf{i}_{b}^{max} + \mathbf{B}_{r}^{t} \mathbf{P}_{load}^{t} \leq \mathbf{B}_{r}^{t} \mathbf{P}_{gen}^{t} \leq \mathbf{i}_{b}^{max} + \mathbf{B}_{r}^{t} \mathbf{P}_{load}^{t} \\ \mathbf{v}^{min} \leq \mathbf{v}^{t} \leq \mathbf{v}^{max} \\ \mathbf{P}_{pr}^{min,t} \leq \mathbf{P}_{pr}^{t} \leq \mathbf{P}_{pr}^{max,t} \\ \mathbf{Q}_{pr}^{min,t} \leq \mathbf{Q}_{pr}^{t} \leq \mathbf{Q}_{pr}^{max,t} \\ \mathbf{0} \leq \mathbf{P}_{ch}^{t} \leq \mathbf{P}_{batt,ch}^{max} \\ \mathbf{0} \leq \mathbf{P}_{dis}^{t} \leq \mathbf{P}_{batt,dis}^{max} \\ S_{batt,i}^{t=1} = S_{batt,i}^{in} \\ S_{batt,i}^{min} \leq S_{batt,i}^{t} \leq x_{batt,i} \\ \eta_{ch,i} \mathbf{P}_{ch,i}^{T} \leq x_{batt,i} - S_{batt,i}^{T} \\ \frac{\mathbf{P}_{dis,i}^{T}}{\eta_{dis,i}} \leq S_{batt,i}^{T} \end{aligned}$$

Where:

- **i**^{max}_b is the vector of the maximal admissible currents in the branches;
- **v**^{min} and **v**^{max} are the vectors of the minimal and maximal admissible voltages at the buses;
- $\mathbf{P}_{pr}^{min,t}$ and $\mathbf{P}_{pr}^{max,t}$ are the vectors of the minimal and maximal level of active power production at the buses;
- $\mathbf{Q}_{pr}^{min,t}$ and $\mathbf{Q}_{pr}^{max,t}$ are the vectors of the minimal and maximal level of reactive power production at the buses;
- **P**^{max}_{batt, dis} is the vector of the maximal admissible power exchanged with the batteries;

The feeder

Since we are using the same variables both for the prosumer and the feeder, we need to fix to zero the values related to batteries and consumption of the first bus (the root connection).

$$P_{Load,0}^{t} = 0$$
$$Q_{Load,0}^{t} = 0$$
$$P_{ch,0}^{t} = 0$$
$$P_{dis,0}^{t} = 0$$

Objective Function

The objective of the optimization problem is to minimize the costs (or maximize the revenues) encountered, over the entire time period, exchanging power with the main grid. If c t el is the price of the electricity and P t 0 is the power exchanged with the grid at time $t \in \{1, ..., T\}$ (positive if sold to the feeder, negative if bought from it), the objective function of the optimization problem can be written as:

$$\min\sum_{t=1}^{T} c_{el}^{t} P_{0}^{t}$$

LP-OPF

The assumptions and approximations introduced until now define the formulation of a Linear Programming of the Optimal Power Flow (LF-OPF) problem:

4.2. OPTIMAL POWER FLOW IN AN EPC

 $\sum^{T} c^{t}_{el} P^{t}_{0}$ minimize (4.8)y $\forall t \in \{1, \ldots T\}:$ subject to $\mathbf{P}_{gen}^{t} = \mathbf{P}_{pr}^{t} + \mathbf{P}_{dis}^{t} - \mathbf{P}_{ch}^{t}$ (4.9) $\sum_{i=0}^{N-1} P_{gen,i}^{t} - \sum_{i=1}^{L} P_{los,j}^{t} - \sum_{i=1}^{L} Q_{los,j}^{t} - \sum_{i=0}^{N-1} P_{load,i}^{t} = 0$ (4.10) $\mathbf{B}_{v}^{t} \begin{bmatrix} \mathbf{P}_{gen}^{t} \\ \mathbf{O}_{em}^{t} \end{bmatrix} - \mathbf{v}^{t} = \mathbf{B}_{v}^{t} \begin{bmatrix} \mathbf{P}_{load}^{t} \\ \mathbf{Q}_{load}^{t} \end{bmatrix} - \mathbf{v}_{s}$ (4.11) $\mathbf{P}_{los}^{t} - \mathbf{L}_{0}^{t} \mathbf{P}_{gen}^{t} \geq -\mathbf{L}_{0}^{t} \mathbf{P}_{load}^{t}$ (4.12) $\mathbf{P}_{los}^{t} + \mathbf{L}_{0}^{t} \mathbf{P}_{gen}^{t} \geq \mathbf{L}_{0}^{t} \mathbf{P}_{load}^{t}$ (4.13) $\mathbf{P}_{los}^{t} - \mathbf{L}_{1}^{t} \mathbf{P}_{gen}^{t} \geq -\mathbf{L}_{1}^{t} \mathbf{P}_{load}^{t} + \mathbf{b}$ (4.14) $\mathbf{P}_{los}^{t} + \mathbf{L}_{1}^{t} \mathbf{P}_{gen}^{t} \ge + \mathbf{L}_{1}^{t} \mathbf{P}_{load}^{t} + \mathbf{b}$ (4.15) $\mathbf{Q}_{los}^{t} - \mathbf{L}_{0}^{t}\mathbf{Q}_{een}^{t} \geq -\mathbf{L}_{0}^{t}\mathbf{Q}_{load}^{t}$ (4.16) $\mathbf{Q}_{los}^{t} + \mathbf{L}_{0}^{t}\mathbf{Q}_{gen}^{t} \geq \mathbf{L}_{0}^{t}\mathbf{Q}_{load}^{t}$ (4.17) $\mathbf{Q}_{los}^{t} - \mathbf{L}_{1}^{t}\mathbf{Q}_{gen}^{t} \geq -\mathbf{L}_{1}^{t}\mathbf{Q}_{load}^{t} + \mathbf{b}$ (4.18) $\mathbf{Q}_{los}^{t} + \mathbf{L}_{1}^{t}\mathbf{Q}_{gen}^{t} \geq +\mathbf{L}_{1}^{t}\mathbf{Q}_{load}^{t} + \mathbf{b}$ (4.19) $-\mathbf{i}_{b}^{max} + \mathbf{B}_{r}^{t}\mathbf{P}_{load}^{t} \leq \mathbf{B}_{r}^{t}\mathbf{P}_{gen}^{t} \leq \mathbf{i}_{b}^{max} + \mathbf{B}_{r}^{t}\mathbf{P}_{load}^{t}$ (4.20) $\mathbf{v}^{min} < \mathbf{v}^{t} < \mathbf{v}^{max}$ (4.21) $\mathbf{P}_{pr}^{min,t} \leq \mathbf{P}_{pr}^{t} \leq \mathbf{P}_{pr}^{max,t}$ (4.22) $\mathbf{Q}_{pr}^{min,t} \leq \mathbf{Q}_{pr}^{t} \leq \mathbf{Q}_{pr}^{max,t}$ (4.23) $0 \leq \mathbf{P}_{ch}^{t} \leq \mathbf{P}_{batt, ch}^{max}$ (4.24) $0 \leq \mathbf{P}_{dis}^t \leq \mathbf{P}_{batt, dis}^{max}$ (4.25) $S_{batt,i}^{t=1} = S_{batt,i}^{in}$ (4.26) $S_{batt,i}^{min} \leq S_{batt,i}^{t} \leq x_{batt,i}$ (4.27) $S_{batt,i}^{t} = S_{batt,i}^{t-1} + \eta_{ch,i} P_{ch,i}^{t-1} - \frac{P_{dis,i}^{t-1}}{\eta_{dis,i}}$ (4.28) $\eta_{ch,i} P_{ch,i}^T \leq x_{batt,i} - S_{batt,i}^T$ (4.29) $\frac{P_{dis,i}^T}{\eta_{dis,i}} \le S_{batt,i}^T$ (4.30) Where y is the set of variables of the optimization problem:

$$\mathbf{y} = \{\mathbf{y}^1, \dots, \mathbf{y}^T\}$$
$$\forall t \in \{1, \dots, T\}:$$
$$\mathbf{y}^t = \{\mathbf{v}^t, \mathbf{P}_{pr}^t, \mathbf{Q}_{pr}^t, \mathbf{P}_{ch}^t, \mathbf{P}_{dis}^t, \mathbf{P}_{los}^t, \mathbf{Q}_{los}^t, \mathbf{S}_{batt}^t\},$$

FBS algorithm The matrices L t 0 ,L t 1 ,B t r and B t v depend on the bus voltages v t , that are initially unknown. The way to get around it, as presented in [33] is to set first the voltages to 1 pu and then to solve iteratively the LP-OPF. After each iteration h, the currents are calculated in the forward stage and the voltages updated in the backward stage. The new voltages are used to evaluate the matrices L t 0 ,L t 1 ,B t r and B t v for the next iteration, until the difference between the values of v of two consecutive iterations is below a certain threshold of tolerance. The FBS-OPF problem presented, optimize the control strategy over all the simulated period, knowing at each step the future prices of electricity, the future load consumption and the future potential power production. Thanks to this information, it is able to decide how to produce, store, buy and sell the electricity in the most efficient way. This is obviously an idealistic situation, since in real world, future is extremely difficult to predict. However, the results obtained simulating realistic scenarios and solving them with this centralized "omniscient" controller, can be useful to produce a learning set for a SL model as the one presented in the chapter 3

5 - Conclusion

This work presented some of the main aspects that revolve around the concept, quite recent, of the Electric Prosumer Communities. It pointed out several times what are the reasons for them to spread worldwide and what could be the challenges that they offer. A snapshot of the technologies associated to distributed generation and energy storage has been provided, demonstrating that many solutions are available to shift from being a consumer to a prosumer. The attention was then moved on the control strategies of a community, in particular on decentralized schemes. A simplified mathematical framework has been presented in order to better contextualize the problem. Power flow analysis and optimal power flow problems have been briefly introduced. We described one possible method to find what the optimal actions of each prosumer are when all the external variables, like potential production, consumption and electricity price are known at every instant. We tried to design a decentralized control scheme using a machine learning approach (more specifically, regression trees) to mimic, at an individual level (using local measurements only), the optimal behavior observed in the centralized solution. Another decentralized control strategy that follows predetermined procedures has been developed to make comparisons. The control schemes were then tested on a case study in three different scenarios. As expected, decentralized control schemes are penalized respect to centralized strategy, when it comes to efficiency. A deeper and wider knowledge of the network is essential to manage adequately the community and to understand what would be the appropriate behavior of single prosumers. Finally, knowing about the simultaneous actions of every prosumers, gives the central entity a better insight of the situation, making possible to put in place cost-effective strategies. Hierarchical control mechanism requires however expensive machinery and sharing personal information such as consumption habits, and it is not that easy to find the optimal strategy with so many unpredictable parameters. The results suggest that a decentralized control scheme relying supervised learning can provide interesting results, but revealed some of its limits. Some expedient that can improve this SL control strategy have been proposed. This thesis work was however performed using several simplification. The mathematical model for the community and for the power flow analysis involved many assumptions in order to reduce the computational cost of the problems, and discrete event simulation can rarely model adequately the dynamics of electric power system, therefore the results of the case study need to be seen in the right perspective. What is for sure is that developing more and more sophisticated methods to tackle the control challenge of micro grids and EPCs is an essential step to make them spread. Designing new decentralized schemes relying on more advanced machine learning techniques, such as Reinforcement Learning (RL), could lead to interesting results, due the ability of that method to self-improve, even when addressing unexpected scenarios.

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